

Designing Optimal Defaults

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- ▶ Behavioral economics gives us lots of new policies to study...
- ▶ ...and it destroys our existing welfare framework.
- ▶ This paper examines this problem for the case of default options.
 - ▶ Retirement savings (Madrian and Shea, 2001; Choi et al 2004; Carroll et al 2009; Chetty et al 2014; Bernheim Fradkin Popov 2016)
 - ▶ Privacy controls (Johnson et al 2002; Acquisti et al 2013)
 - ▶ Health (Chapman et al. 2010)
 - ▶ Student loan repayment

The Classical View

- ▶ Classic revealed preference theory equates choice with welfare

$$c_i(X, S) = \arg \max_{x \in S} u_i(x) \quad (1)$$

$$w_i = u_i(c_i(x, S)) \quad (2)$$

- ▶ can add prices, endowments, taxes, etc.

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- ▶ then default effects are observed
 - ▶ *rationalization*: modify (1) (add to S , $u(\cdot)$)
 - ▶ Psychological costs, transaction costs, switching costs, etc.
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 - ▶ But then does (2) still hold?

Rationalizing Default Effects

$$v_i(x(d), d) = u_i(x(d)) - \gamma_i 1\{x(d) \neq d\} \quad (3)$$

- ▶ γ_i is an "as-if" cost.

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- ▶ Yes: need a new rationalization for every behavioral finding
- ▶ But maybe the old normative model was correct?
- ▶ Leads to controversy over default policies
- ▶ Related problems for other behavioral phenomena

This Paper

- ▶ Introduce a simple model of optimal defaults
 - ▶ *Parameterize* normative ambiguity
- ▶ Show that it nests several positive models
- ▶ Characterize welfare effects of default policies
 - ▶ Building towards sufficient statistics...
- ▶ Data?
- ▶ Lessons for other policy problems?

Part 1

A Simple Model of Defaults and Welfare

Setup

- ▶ Behavior $x_i(d)$ given by:

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- ▶ $\rho_i \in [0, 1]$: share of costs that are "normatively relevant."

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- ▶ Utilitarian social welfare $W_i(d) = \int_i w_i(x_i(d), d) di$
- ▶ Note: assuming a varily simple as-if cost function, could in principle be relaxed.

Part 2

Relationship to Positive Theory

Positive Theories: Classic Rationality

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- ▶ The end.
- ▶ ...but you could argue that part of γ_i 's are psychological costs, maybe should be discarded? $\implies \rho_i \leq 1$.

Positive Theories: Present Bias (Q-HD, Laibson 1997)

- ▶ Present bias can magnify small up-front costs (Carrol et al 2009)
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- ▶ Long-run ($\beta = 1$) view of welfare: $\rho_i = \beta_i$.

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- ▶ Long-run ($\beta = 1$) view of welfare: $\rho_i = \beta_i$.
- ▶ Short-run view of welfare: $\rho_i = 1$.
- ▶ Note: with the right variation, δ_i, β_i are identified, but the "right" view of welfare is still unknown.

Positive Theories: Anchoring/Status Quo

- ▶ Give extra utility ω_i to default option:

$$v_i(x, d) = u_i(x) + \omega_i 1\{x_i \neq d\}$$

- ▶ Assumes no spillovers to "near-default" choices
- ▶ Consistent with aggregate evidence on 401k [▶ illustration](#)
- ▶ Could relax with more sophisticated as-if cost function

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- ▶ Then $\gamma_i \equiv -\omega_i$
 - ▶ Many think $\rho_i = 0$, one could argue otherwise (was default deliberately chosen?)

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- ▶ Behavior: $\max_{x \in \Gamma_i(d)} u_i(x)$

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- ▶ Endogenize Γ_i to close the model:
- ▶ Rationally chosen with full information $\implies \rho = 1$
 - ▶ A planner-doer model (Fudenberg and Levine, 2006)
 - ▶ Normatively equivalent to neoclassical model

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- ▶ Rationally chosen with less than full information??
 - ▶ ρ depends on how accurate beliefs are?
 - ▶ Some $\rho_i > 1$?

Takeaways

- ▶ This simple framework nests many positive models
- ▶ Models differ by ρ_i 's
- ▶ Could easily combine some of these models.
- ▶ \implies At least any value $\rho \in [0, 1]$ is plausible, maybe even $\rho > 1$.

Part 3

Characterizing Optimal Policy

Binary Case

- ▶ Consider a fixed binary menu $S = \{0, 1\}$
- ▶ Monotonicity: $\gamma_i \geq 0$ for all i implies $(x_i(0), x_i(1)) \neq (1, 0)$
- ▶ Let $\Delta u_i = u_i(1) - u_i(0)$

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Proposition:

$$W(1) - W(0) = E[\rho_i \gamma_i | 1, 1] p_{11} - E[\rho_i \gamma_i | 0, 0] p_{00} + E[\Delta u_i | 0, 1] p_{01}$$

Binary Case

Proposition: Suppose

- ▶ $\rho_i \gamma_i \perp \Delta u_i$.
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- ▶ Size of $W(1) - W(0)$ *does* depend on ρ

Building Toward the General Case

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- ▶ Let $x_i^* = \arg \max_{x \in S} u_i(x)$
- ▶ Identification: $a_i(d) = 1 \implies x_i = x_i^*$
 - ▶ Falsifiable for any i with ideal dataset

When Might ρ_i Matter For Policy?

Case 1: Active choices:

- ▶ Suppose there is a default d^A that is so bad that $a_i(d) = 1$ for every i (Carroll et al 2009)
- ▶ Further suppose $\rho_i = 0$ for all i .

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- ▶ Then $d = x_i^*$ is plainly the optimal default, regardless of ρ .

Some intuition

Normative ambiguity appears to occur when

- ▶ γ_i is large,
- ▶ the space of possible defaults (S) is rich, and/or
- ▶ optimal choices (x_i^*) are more heterogeneous.

Effect of a Change in the Default

Consider two defaults: (d_0, d_1) . Define:

- ▶ Always active (AA): $a_i(d_0) = a_i(d_1) = 1$

$$u_i(x^*) - \max\{u_i(d_0), u_i(d_1)\} \geq \gamma_i$$

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- ▶ Become passive (BP): $a_i(d_0) = 1; a_i(d_1) = 0$

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- ▶ Become active (BA): $a_i(d_0) = 0; a_i(d_1) = 1$

$$u_i(x^*) - u_i(d_0) < \gamma_i < u_i(x^*) - u_i(d_1)$$

The Welfare Effect of a Default Change

Proposition:

$$\begin{aligned}W(d_1) - W(d_0) &= E[u_i(x^*) - u_i(d_0) - \rho\gamma_i|BA]p_{BA} \\ &- E[u_i(x^*) - u_i(d_1) - \rho\gamma_i|BP]p_{BP} \\ &+ E[u_i(d_1) - u_i(d_0)|AP]p_{AP}\end{aligned}$$

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Remarks:

- ▶ Welfare of AA group is irrelevant
- ▶ Need to further characterize when $sign(W(d_1) - W(d_0))$ depends on ρ_i 's.
- ▶ Intuitively ρ will only matter if BA and BP have very different γ or u

The Welfare Effect of a Default Change

Proposition:

$$\begin{aligned}W(d_1) - W(d_0) &= E[u_i(x^*) - u_i(d_0) - \rho\gamma_i|BA]p_{BA} \\ &\quad - E[u_i(x^*) - u_i(d_1) - \rho\gamma_i|BP]p_{BP} \\ &\quad + E[u_i(d_1) - u_i(d_0)|AP]p_{AP}\end{aligned}$$

Remarks:

- ▶ Welfare of AA group is irrelevant
- ▶ Need to further characterize when $sign(W(d_1) - W(d_0))$ depends on ρ_i 's.
- ▶ Intuitively ρ will only matter if BA and BP have very different γ or u

Welfare Effect of a *Marginal* Default Change

- ▶ Suppose $S = [a, b] \subseteq \mathbb{R}$
- ▶ Using TSA the previous proposition becomes:

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- ▶ With $\rho_i \ll 1$ BA and BP groups become much more important
- ▶ Can prove a similar proposition to before with $\frac{du_i}{dx} \Big|_{x=d}$ symmetric, single-peaked, independent of ρ_i, γ_i .

CONJECTURES

When does $\text{sign}(\Delta W)$ depend on ρ_i 's?

- ▶ when Δu_i has a highly asymmetric distribution, and
- ▶ when γ_i 's are large and correlated with Δu_i
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Identifying distribution of $\gamma_i, u_i(\cdot)$ (parameterized) is a tractable RP problem

- ▶ but no model can identify ρ .
- ▶ Components of γ might be separated empirically, e.g. present bias,
- ▶ but discarding some of them still requires normative judgement.

Part 4

Conclusions

Optimal Policy and Normative Ambiguity

- ▶ When ρ is irrelevant for policy
 - ▶ e.g. kinks in budget for 401(k) \implies optimal default will tend to be at 0 or max employer match (Bernheim Fradkin Popov 2015).

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 - ▶ But we can still tell policymakers about the map from ρ 's to optimal policy.
 - ▶ e.g. if you think $\rho = 0$, maximizing active choices looks great; if you think $\rho = 1$, maybe minimize opt-outs.

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Public economics employs two types of optimal policy analysis

- ▶ Efficiency arguments (Kaldor, 1939; Hicks, 1939, 1940)
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Can a similar distinction lead to a broad consensus about optimal defaults...about behavioral welfare economics?

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 - ▶ Express "true" welfare as a weighted sum of utility functions that rationalize behavior in different frames, weights $\equiv \rho$.
 - ▶ Temptation: u vs $u + v$
 - ▶ Present bias: $\beta = 1$ and $\beta < 1$
 - ▶ Gain/loss framing? Others?

THANK YOU!

Questions/comments: dreck@umich.edu

Defaults with richer choice sets: Application

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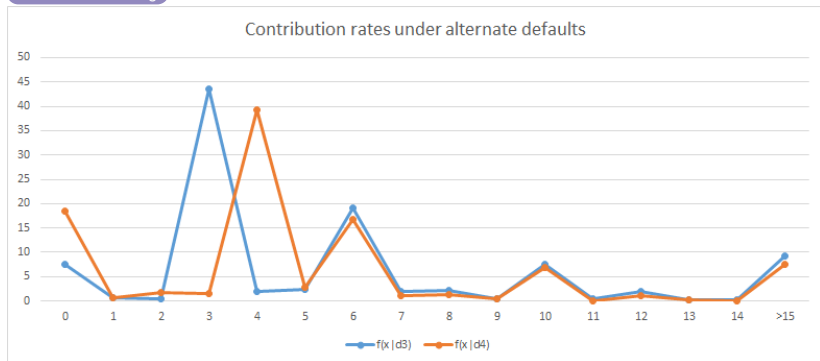
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- ▶ Enrollment contributions of newly eligible workers before and after switch
- ▶ 15% max contribution
- ▶ Large kink at 6% from 1:1 employer match

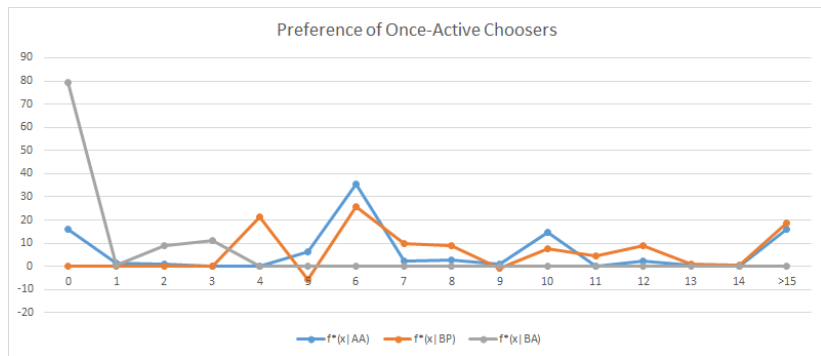
Defaults with richer choice sets: Aggregate data

▶ back to anchoring



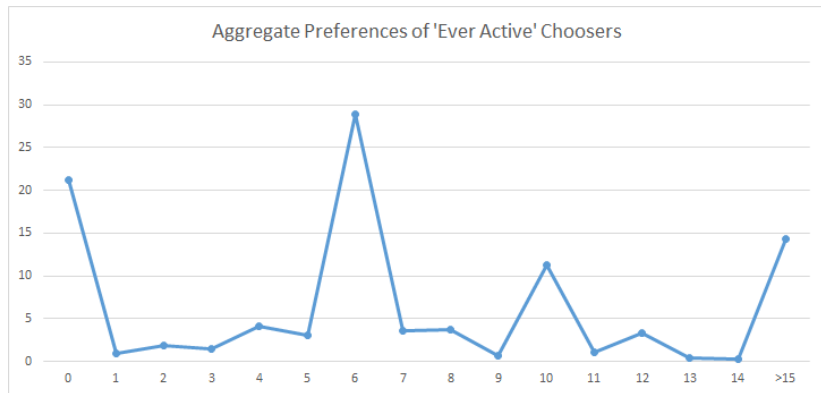
▶ back to next steps

Defaults with richer choice sets: Identified distributions



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Defaults with richer choice sets: Identified distributions



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